



E-Module on NORMALIZATION

Class:- BA/BSC(Computer Application)-V Sem

Subject:- Database Management System

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First Normal Form

- A table is in the first normal form iff
 - The domain of each attribute contains only ***atomic values***, and
 - The value of each attribute contains only a ***single value*** from that domain.

In layman's terms. it means every column of your table should only contain ***single values***

Example

- For a library

| Patron ID | Borrowed books |
|-----------|----------------|
| C45 | B33, B44, B55 |
| C12 | B56 |

1-NF Solution

| Patron ID | Borrowed book |
|-----------|---------------|
| C45 | B33 |
| C45 | B44 |
| C45 | B33 |
| C12 | B56 |

Example

- For an airline

| Flight | Weekdays |
|--------|----------------|
| UA59 | Mo We Fr |
| UA73 | Mo Tu We Th Fr |

1NF Solution

| Flight | Weekday |
|--------|---------|
| UA59 | Mo |
| UA59 | We |
| UA59 | Fr |
| UA73 | Mo |
| UA73 | We |
| ... | ... |



Implication for the ER model

- Watch for entities that can have multiple values for the same attribute
 - Phone numbers, ...
- What about course schedules?
 - MW 5:30-7:00pm
 - Can treat them as *atomic time slots*

Functional dependency

Let X and Y be *sets* of attributes in a table T

- Y is **functionally dependent** on X in T **iff** for each set $x \in R.X$ there is precisely one corresponding set $y \in R.Y$
- Y is **fully functional dependent** on X in T if Y is functional dependent on X and Y is not functional dependent on any proper subset of X

Example

■ Book table

| BookNo | Title | Author | Year |
|--------|-----------|-------------|------|
| B1 | Moby Dick | H. Melville | 1851 |
| B2 | Lincoln | G. Vidal | 1984 |

Author attribute is:

- ***functionally dependent*** on the pair { BookNo, Title }
- ***fully functionally dependent*** on BookNo

Why it matters

- table BorrowedBooks

| BookNo | Patron | Address | Due |
|--------|-----------|-------------------|---------|
| B1 | J. Fisher | 101 Main Street | 3/2/15 |
| B2 | L. Perez | 202 Market Street | 2/28/15 |

Address attribute is

- **functionally dependent** on the pair { BookNo, Patron }
- **fully functionally dependent** on Patron

Problems

- Cannot insert new patrons in the system until they have borrowed books
 - *Insertion anomaly*
- Must update all rows involving a given patron if he or she moves.
 - *Update anomaly*
- Will lose information about patrons that have returned all the books they have borrowed
 - *Deletion anomaly*

Armstrong inference rules (1974)

■ ***Axioms:***

- Reflexivity: if $Y \subseteq X$, then $X \rightarrow Y$
- Augmentation: if $X \rightarrow Y$, then $WX \rightarrow WY$
- Transitivity: if $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

■ ***Derived Rules:***

- Union: if $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
- Decomposition: if $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
- Pseudotransitivity: if $X \rightarrow Y$ and $WY \rightarrow Z$, then $XW \rightarrow Z$

Armstrong inference rules (1974)

- Axioms are both

- **Sound:**

- when applied to a set of functional dependencies they only produce dependency tables that belong to the transitive closure of that set

- **Complete:**

- can produce all dependency tables that belong to the transitive closure of the set

Armstrong inference rules (1974)

- Three last rules can be derived from the first three (the axioms)
- Let us look at the ***union rule***:
if $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
- Using the first three axioms, we have:
 - if $X \rightarrow Y$, then $XX \rightarrow XY$ same as $X \rightarrow XY$ (2nd)
 - if $X \rightarrow Z$, then $YX \rightarrow YZ$ same as $XY \rightarrow YZ$ (2nd)
 - if $X \rightarrow XY$ and $XY \rightarrow YZ$, then $X \rightarrow YZ$ (3rd)

Second Normal Form

- A table is in 2NF iff
 - It is in 1NF and
 - no non-prime attribute is dependent on any proper subset of any candidate key of the table
- A ***non-prime attribute*** of a table is an attribute that is not a part of any candidate key of the table
- A ***candidate key*** is a minimal superkey

Example

- Library allows patrons to request books that are currently out

| BookNo | Patron | PhoneNo |
|--------|-----------|----------|
| B3 | J. Fisher | 555-1234 |
| B2 | J. Fisher | 555-1234 |
| B2 | M. Amer | 555-4321 |

Example

- Candidate key is {BookNo, Patron}
- We have
 - Patron → PhoneNo
- Table is not 2NF
 - Potential for
 - Insertion anomalies
 - Update anomalies
 - Deletion anomalies

2NF Solution

- Put telephone number in separate Patron table

| BookNo | Patron |
|--------|-----------|
| B3 | J. Fisher |
| B2 | J. Fisher |
| B2 | M. Amer |

| Patron | PhoneNo |
|-----------|----------|
| J. Fisher | 555-1234 |
| M. Amer | 555-4321 |



Third Normal Form

- A table is in 3NF iff
 - it is in 2NF and
 - all its attributes are determined only by its candidate keys and not by any non-prime attributes

Example

- Table BorrowedBooks

| BookNo | Patron | Address | Due |
|--------|-----------|-------------------|---------|
| B1 | J. Fisher | 101 Main Street | 3/2/15 |
| B2 | L. Perez | 202 Market Street | 2/28/15 |

- Candidate key is BookNo
- Patron → Address

3NF Solution

- Put address in separate Patron table

| BookNo | Patron | Due |
|--------|-----------|---------|
| B1 | J. Fisher | 3/2/15 |
| B2 | L. Perez | 2/28/15 |

| Patron | Address |
|-----------|-------------------|
| J. Fisher | 101 Main Street |
| L. Perez | 202 Market Street |

Another example

- Tournament winners

| Tournament | Year | Winner | DOB |
|----------------------|------|----------------|---------------|
| Indiana Invitational | 1998 | Al Fredrickson | 21 July 1975 |
| Cleveland Open | 1999 | Bob Albertson | 28 Sept. 1968 |
| Des Moines Masters | 1999 | Al Fredrickson | 21 July 1975 |

- Candidate key is {Tournament, Year}
- Winner → DOB

Boyce-Codd Normal Form

- Stricter form of 3NF
- A table T is in BCNF iff
 - for every one of its non-trivial dependencies $X \rightarrow Y$, X is a super key for T
- Most tables that are in 3NF also are in BCNF

Example

| Manager | Project | Branch |
|---------|---------|---------|
| Alice | Alpha | Austin |
| Alice | Delta | Austin |
| Carol | Alpha | Houston |
| Dean | Delta | Houston |

- We can assume
 - Manager \rightarrow Branch
 - {Project, Branch} \rightarrow Manager

Example

| <u>Manager</u> | <u>Project</u> | Branch |
|----------------|----------------|---------|
| Alice | Alpha | Austin |
| Bob | Delta | Houston |
| Carol | Alpha | Houston |
| Alice | Delta | Austin |

- Not in BCNF because $\text{Manager} \rightarrow \text{Branch}$ and Manager is not a superkey
- Will decomposition work?

A decomposition (I)

| <u>Manager</u> | Project |
|----------------|---------|
| Alice | Alpha |
| Bob | Delta |
| Carol | Alpha |
| Alice | Delta |

| <u>Manager</u> | Branch |
|----------------|---------|
| Alice | Austin |
| Bob | Houston |
| Carol | Houston |

- Two-table solution does not preserve the dependency $\{\text{Project, Branch}\} \rightarrow \text{Manager}$

A decomposition (II)

| <u>Manager</u> | Project |
|----------------|---------|
| Alice | Alpha |
| Bob | Delta |
| Carol | Alpha |
| Alice | Delta |
| Dean | Delta |

| <u>Manager</u> | Branch |
|----------------|---------|
| Alice | Austin |
| Bob | Houston |
| Carol | Houston |
| Dean | Houston |

- Cannot have two or more managers managing the same project at the same branch



Multivalued dependencies

- Assume the column headings in a table are divided into three disjoint groupings X , Y , and Z
- For a particular row, we can refer to the data beneath each group of headings as x , y , and z respectively

Multivalued dependencies

- A ***multivalued dependency*** $X \twoheadrightarrow Y$ occurs if
 - For any x_c actually occurring in the table and the list of all the $x_c y z$ combinations that occur in the table, we will find that x_c is associated with the same y entries regardless of z .
- A ***trivial multivalued dependency*** $X \twoheadrightarrow Y$ is one where either
 - Y is a subset of X , or
 - Z is empty ($X \cup Y$ has all column headings)

Fourth Normal Form

- A table is in 4NF iff
 - For every one of its non-trivial multivalued dependencies $X \twoheadrightarrow Y$, X is either:
 - A candidate key or
 - A superset of a candidate key

Example from Wikipedia

| Restaurant | Pizza | DeliveryArea |
|---------------|-------------|--------------|
| Pizza Milano | Thin crust | SW Houston |
| Pizza Milano | Thick crust | SW Houston |
| Pizza Firenze | Thin crust | NW Houston |
| Pizza Firenze | Thick crust | NW Houston |
| Pizza Milano | Thin crust | NW Houston |
| Pizza Milano | Thick crust | NW Houston |

Discussion

- The table has no non-key attributes
 - Key is { Restaurant, Pizza, DeliveryArea}
- Two non-trivial multivalued dependencies
 - Restaurant \Rightarrow Pizza
 - Restaurant \Rightarrow DeliveryArea

since each restaurant delivers the same pizzas to all its delivery areas

4NF Solution

- Two separate tables

| Restaurant | DeliveryArea |
|---------------|--------------|
| Pizza Milano | SW Houston |
| Pizza Firenze | NW Houston |
| Pizza Milano | NW Houston |

| Restaurant | Pizza |
|---------------|-------------|
| Pizza Milano | Thin crust |
| Pizza Milano | Thick crust |
| Pizza Firenze | Thin crust |
| Pizza Firenze | Thick crust |

Join dependency

- A table T is subject to a **join dependency** if it can always be recreated by **joining** multiple tables each having a subset of the attributes of T
- The join dependency is said to be **trivial** if one of the tables in the join has all the attributes of the table T
- *Notation:* $\{ A, B, \dots \}$ on T

Fifth normal form

- A table T is said to be 5NF iff
 - Every non-trivial join dependency in it is implied by its candidate keys
- A join dependency $*\{A, B, \dots, Z\}$ on T is implied by the candidate key(s) of T if and only if each of A, B, \dots, Z is a superkey for T

An example

| <i>Store</i> | <i>Brand</i> | <i>Product</i> |
|--------------|--------------|----------------|
| Circuit City | Apple | Tablets |
| Circuit City | Apple | Phones |
| Circuit City | Toshiba | Laptops |
| CompUSA | Apple | Laptops |

- Note that Circuit City sells Apple tablets and phones but only Toshiba laptops